Till läraren



Välkommen till Kängurutävlingen – Matematikens hopp 2024 *Cadet*

- Tävlingen genomförs under perioden 21 mars 5 april. *Uppgifterna får inte användas tidigare*.
- Sista dag f\u00f6r redovisning av antalet deltagare \u00e4r den 12 april. Du f\u00e4r d\u00e4 tillg\u00e4ng till facit och ett kalkylblad d\u00e4r du matar in elevernas svar och sedan f\u00e4r du en sammanst\u00e4llning av klassens resultat.
- Redovisa resultatet senast 30 april.
- Tävlingen är individuell och eleverna får arbeta i 60 minuter. De tre delarna ska genomföras vid ett och samma tillfälle.
- Eleverna behöver ha tillgång till papper för att kunna göra anteckningar och figurer. Linjal behövs inte
- Miniräknare eller sax får inte användas. Observera att telefoner, datorplattor och datorer inte heller får användas.
- Läs igenom problemen själv i förväg så att eventuella oklarheter kan redas ut.
- Kontrollera att kopiorna blir tillräckligt tydliga så att nödvändiga detaljer syns.
- Besök Kängurusidan på ncm.gu.se/kanguru där vi publicerar eventuella rättelser och ytterligare information. Där finns också information om hur kalkylbladet fungerar.
- Samla in problemformulären efter tävlingen. Problemen får inte spridas utanför klassrummet förrän efter 30 april, men ni får gärna arbeta med problemen i klassen.

Mikael Passares stipendium

Mikael Passare (1959–2011) var professor i matematik vid Stockholms universitet. Han hade ett stort intresse för matematikundervisning på alla nivåer och var den som tog initiativ till Kängurutävlingen i Sverige. Mikael Passares minnesfond har instiftat ett stipendium för att uppmärksamma elevers goda matematikprestationer. Information om hur du nominerar elever kommer tillsammans med facit och kommentarer.

Lycka till med årets Känguru!

e-post: kanguru@ncm.gu.se

För administrativa frågor, vänd dig till Ann-Charlotte Forslund: ann-charlotte.forslund@ncm.gu.se 031–786 69 85

För innehållsfrågor, vänd dig till Ulrica Dahlberg eller Johan Häggström: ulrica.dahlberg@ncm.gu.se johan.haggstrom@ncm.gu.se



Svarsblankett

Markera ditt svar i rätt ruta

Uppgift	Α	В	С	D	E	Poäng
1						
2						
3						
4						
5						
6						
7						
8						
9						
10						
11						
12						
13						
14						
15						
16						
17						
18						
19						
20						
21						
22						
23						
24						
				SUI	MMA	

Namn:	 	
rz1		
Klass:	 	

Kängurutävlingen – Matematikens hopp 2024 Cadet



Three points problems

1 A string is laid so that it forms a horizontal figure eight.



Which of the following strings cannot be transformed into the string on the right without cutting?





В



C



D

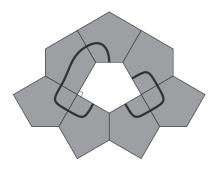


Е



[Germany]

2 A shape is made of equal-sized pentagonal tiles.



Which of the following tiles can be placed in the space in the shape to produce two closed curves?





В



C



D



Е



[Slovenia]

3 The first diagram shows a rhombus. The area of the first diagram is increased by adding two right-angled triangles, as shown.





By what percentage has the area increased?

A 20%

B 25%

C 30%

D 40%

E 50%

[Spain]

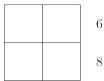


4	What is t	he value of the	e expression?	$\frac{20\cdot 24}{2\cdot 0 + 2\cdot 4}$		
	A 12	В 30	C 48	D 60	E 120	[Uganda]
5			orners of a regular		,	
	A 8	В 9	C 11	D 12	E 15	[Germany]
6			marked 1, 5 and 11, de to make a four-			1 5 11
	How man	ny different fou	ır-digit numbers	can she make	?	
	A 3	B 4	C 6	D 8	E 9	[Netherlands]
7	 Alva lik Bo likes Camilla Dan like Eva like The fruit type of free 	es apples apples, cherri likes grapes, c es apples, grap es apples and cl	es, strawberries and cherries and cherries herries and cherries herries at everyone gets a	nd bananas ries and bana	nnas	erries and bananas. veryone gets a
	A Alva	В Во	C Camilla	D Dan	E Eva	[Switzerland]
8	children.	According to t	notice for an eleva the weight restric ator with nine ad	tions, what i	-	
	A 3	B 4	C 5	D 6	E 8	[Ukraine]



Four points problems

Four different positive integers are placed on a grid and then covered up. The products of the integers in each row and in each column are shown in the diagram.



4

What is the sum of the four integers?

A 10

B 12

C 13

D 14

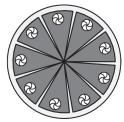
E 15

[Australia]

12

10 Carina baked a cake and cut it into ten equal pieces. She ate one piece and then arranged the remaining pieces evenly, as shown.

What is the size of the angle between any two pieces?



A 5°

B 4°

 $C 3^{\circ}$

D 2°

E 1°

[Germany]

11 Werner can make a 4×4 square, where the sum of the numbers in all four rows and all four columns is the same, from the three pieces shown and one further piece.



2 1 3

	2	
3	1	2

Which of the following pieces is needed to complete his square?

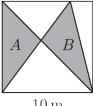
1 2 1

[Germany]

12 A square has side-length 10 m. It is divided into parts by three straight line segments, as shown.

The areas of the two shaded triangles are A and B.

What is the value of A - B?



 $10\,\mathrm{m}$

 $A O m^2$

 $B 1 m^2$

 $C 2 m^2$

 $D 5 m^2$

 $E 10 \, m^2$

[Greece]

13 Paula the penguin goes fishing every day and always brings back twelve fish for her two chicks. Each day, she gives the first chick she sees seven fish and gives the second chick five fish, which they eat. In the last few days one chick has eaten 44 fish.

How many has the other chick eaten?

A 34

B 40

C 46

D 52

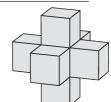
E 58

[United Kingdom]



14 Johan had a large number of identical cubes. He made the structure on the right by taking a single cube and then sticking another cube to each face. He wants to make an extended structure in the same way so that each face of his original structure will have a cube stuck to it.





How many extra cubes will he need to complete his extended structure?

A 18

B 16

C 14

D 12

E 10

[Brazil]

15 Gerard cuts a large rectangle into four smaller rectangles. The perimeters of three of these smaller rectangles are 16, 18 and 24, as shown in the diagram.

?

18

16

24

What is the perimeter of the fourth small rectangle?

A 8

B 10

C 12

D 14

E 16

[Netherlands]

Water makes up 80 percent of the mass of fresh mushrooms. However, water makes up only 20 percent of the mass of dried mushrooms.

By what percentage does the mass of the mushroom decrease during drying?

A 60%

B 70%

C 75%

D 80%

E 85%

[Hungary]

Five points problems

17 Teri the tiler is planning to make a large, square mosaic floor with a repeating pattern, using hexagonal and triangular tiles, arranged as shown in the diagram. She thinks she will use 3000 hexagonal tiles to make the whole floor.



Approximately, how many triangular tiles will she need?

A 1000

B 1500

 C_{3000}

D 6000

E 9000

[Finland]

- 18 Nine cards numbered from 1 to 9 were placed facedown on the table. Aleksa, Bart, Clara and Deindra each picked up two of the cards.
 - Aleksa said "My numbers add up to 6".
 - Bart said "The difference between my numbers is 5".
 - Clara said "The product of my numbers is 18".
 - Dennis said "One of my numbers is twice the other one".

All four made a true statement. Which number was left on the table?

A 1

В 3

C 6

D 8

E 9

[Vietnam]



19 The digits 0–9 can be drawn with horizontal and vertical segments, as shown. Greg chooses three different digits. In total, his digits have 5 horizontal segments and 10 vertical segments.



What is the sum of his three digits?

A 9

B 10

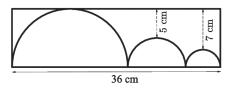
C 14

D 18

E 19

[Finland]

20 The diagram shows three semi-circles inside a rectangle. The middle semi-circle touches the other two semi-circles which, in turn, each touch a shorter side of the rectangle. The largest semi-circle also touches one of the longer sides of the rectangle. The shortest distances from that side of the rectangle to the other two semi-circles are 5 cm and 7 cm respectively, as shown



What is the perimeter, in cm, of the rectangle?

A 82 cm

B 92 cm

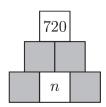
C 96 cm

D 108 cm

E 120 cm

[Catalonia]

21 Donald wants to complete the diagram so that each box in the middle and top rows will contain the product of the values in the two boxes below it and each box contains a positive integer. He wants the value in the top box to be 720.



How many different values can the integer *n* take?

A 1

B 4

 C_{5}

D 6

E 8

[Türkiye]

22 Farmer Barbro is selling chicken and duck eggs. She has baskets holding 4, 6, 12, 13, 22, and 29 eggs. Her first customer buys all the eggs in one basket. Barbro notices that the number of chicken eggs she has left is twice the number of duck eggs.

How many eggs did the customer buy?

A 4

B 12

C 13

D 22

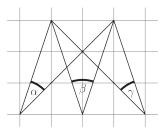
E 29

[Hungary]



23 Three angles α , β and γ are marked on squared paper, as shown.

What is the value of $\alpha + \beta + \gamma$?



A 60°

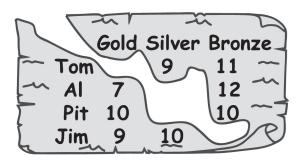
B 70°

C 75°

D 90°

E 120°

24 Captain Flint asked four of his pirates to write on a piece of paper how many gold, silver and bronze coins were in the treasure chest. Their responses are shown in the diagram but unfortunately part of the paper was damaged. Only one of the four pirates told the truth. The other three lied in all their answers. The total number of coins is 30.



Who told the truth?

A Tom

B Al

C Pit

D Jim

E We cannot be sure

[Greece]